Vedic Mathematics

Indian Mathematics from Vedic Period until today is 'Vedic Mathematics'

> Ravi Kumar lyer Mob. +91 8076 4843 56

Vedic Mathematics

I am sorry I am not able to meet you Physically. But once the pandemic is over, let us meet and learn VM properly. Today is only a TRILER

I need your cooperation If possible pl sit with your school going children above the age of 12. They pick up very quickly

I have conducted VM workshops in many leading universities in USA, Canada, Holland, Norway, Australia, New Zealand etc. Also in Royal Society

My 5 Sessions on VM in Radio Sydney won maximum attendance award

ravisydney@yahoo.com, www.hindugenius.blogspot.com

You Tend to hear The Worst 5% of the Indian Story 95% of the Time»

Quotes on Indian Mathematics



We owe a lot to Indians, who taught us how to count, without which no worthwhile scientific discovery could have been made.

Albert Einstein

Albert Einstein Culver Pictures, Inc.

Let Noble Thoughts come from all directions. Rig Veda

Ancient Vedic Shloka over 5,000 years back

"Om purna mada purna midam Purnaat purnam udachyate Purnasya purnam adaaya Purnam eva vasishyate Om shanti shanti shantih" (Isha Upanishad)



Which translates into:

Guillaume de l'Hôpital 1661- 1704 France, Paris INFINITY ÷ ÷ INFINITY = INFINITY

"That is the whole, this is the Whole; from the Whole, the Whole arises; taking away the Whole from the Whole, the Whole remains" (Replace Whole by Infinity) Great Mathematicians of Vedic Period Indian Mathematics from Vedic Period until today is 'Vedic Mathematics'

How old is Vedic Civilization ??

How old is Vedic Civilization ??



Thomas Alva Edison (1847 – 1931)

Gramaphone 1877

Max Müller (1823 – 1900)

अग्निमीळे पुरोहितं यज्ञस्य देवं रत्वीजम। होतारं रत्नधातमम॥ aghnimīle purohitam yajñasya devam rtvījam। hotāram ratnadhātamam॥ **An hmv**

I worship Agni who is the priest, the one who leads us from the front, who is the deity subject matter of a ritual, a yajna who is the one who makes the formal invocations in the yajna who is the source, storehouse and the bestower of all wealth, gems, precious stones etc 1-1-1 of Rigvedam.

How old is Vedic Civilization ?? Saraswati Civilization 8,000 BC ? !







NADISTUTI hymn in the Rigveda (10.75)

RV 7.95.1-2,

TANDYA BRAHMANA and the JAIMINIYA BRAHMANA, as well as the Mahabharata, mention that the Sarasvati DRIED UP IN A DESERT.

1ST Golden Age of Indian Science & Technology Scientists 3,000 Years before





Dhanwantari, Charaka, Sushruta Medical Science including Plastic Surgery, Nano Technology, Veterinary Science, Botany, Pharmacy,







Rishi Bharadwaj, Kapil, Kanad

Vimana Shastra or Space Vehicles, Cosmology or Creation of Universe, Nuclear Physics & Chemistry



War Techniques, Missiles, War Techniques, Architecture, Artha Shastra Yoga, Meditation, Grammar, Ayurveda

BAUDHAYANA THE ORIGINAL MATHEMATICIAN BEHIND PYTHAGORAS THEOREM



Pāņini Father of Linguistics & World's First Geek



Who is Pingala!

Pingala, Fathe

of Binary

Numerals



Bhu Gol (Geography); Ja Gata (It Moves)



- •Varaha (Boar, Pig) Avtar saves Earth
- •Shape of Earth is ROUND
 - •West only after Apollo XI (July 20, 1969) West only after Apollo – XVII Earth Photos (Dec 6, 1972)







Earth Rotates on its own axis and revolves around the Sun 1543 Copernicus

Ja Gata – That which moves NAVAGRAHA

Jai JAGADISHA Hare





AMAVASYA Lord Krishna doing Tarpanam

Hindus Contribution to Calendar Science







Nyayiru
Thingal
Sevvai
GURU
Shani

•Jyeshtha













Carl
Sagan
Cosmos
Cosmology



•Bhu-Golam,

•Ananta Koti Brahmanda m

Jyeshtha Nakshatra = Antares





•JYESTHA or Elder / Biggest Star It is just a point in the sky

•Antares or Alpha Scorpii 17th brightest star in the nighttime sky

•550 light years away

•Radius is 883 times that of Sun Most Massive star / BIGGEST Star ~70 Crore times sun

Sapta Rishi = Ursa Major





•The present, seventh Manvantara - the interval of Vaivasvata Manu

•Kashyapa, Atri, Vashishtha, Vishvamitra, Gautama, Jamadagni, Bharadvaja

•Vasishtha is accompanied by his wife, the faint companion star Arundhati (Alcor/80 Ursa Majoris).

Indian Name	Bayer Desig	Western Name
Kratu	α UMa	Dubhe
Pulaha	β UMa	Merak
Pulastya	y UMa	Phecda
Atri	δ UMa	Megrez
Angiras	εUMa	Alioth
Vasishtha	ζUMa	Mizar
Bhrigu	η UMa	Alkaid

•In Hinduism, Ursa Major is known as Saptarshi, each of the stars representing one of the Saptarshis or Seven Sages viz. Bhrigu, Atri, Angirasa, Vasishta, Pulastya, Pulalaha and Kratu. The fact that the two front stars of the constellations point to the pole star is explained as the boon given to the boy sage Dhruva by Lord Vishnu.

•https://www.youtube.com/watch?v=_yNeuyaGO_E

•Khurshed Batliwala Technology of Spirituality¹³

Mathematics in Vedic Period



Grand Fathers of Computer Science Panini Backus Noir Form

√2



= 1 + 1/3 + 1/3x4 - 1/3x4x34= 577 / 4081.414216

Yajyavalkya, Apastambh, Katyayan, Manava

Shulbha Sutras, Pythagoras Theorem, Triplets, Square Root of 2 Circling the Square

108 = Diameter of Sun Diameter of Earth

- = Distance between earth and Sun diameter of Sun
- = Distance between Moon and Earth Diameter of Moon

Mathematicians from Maharashtra



Magical number 6174 Kaprekar's constant, let's share it with others



Dattaraya Ramchandra Kaprekar (1905–1988) was an Indian recreational mathematician who described several classes of natural numbers including the Kaprekar, Harshad and Self numbers and discovered the Kaprekar constant, named after him. Despite having no formal postgraduate training and working as a schoolteacher, he published extensively.

- He was born in 1957 in Guador.

- + An policy applying the second property of the second sec
- He invested the First providing polycomial bing algorithm. For interve programming also intervent on the interver prior prior polycol.
- Homoritan way a professor at the Tota hybridate of Purplaneted Several in Rumbal Prom 1998 to 2003
- + see was briefly the ministric advisor to the chairmon of the 11/19 group.
- Apartparker worked on a new ordpletture for newcomparting, baved on respect / how highe geometry, expected, projective geometry over Righe Relar.
- He gave a four-perti verier of lecturer at FOCI) 20H (Four-picture) of Computational (flatthyripidic/) stated "Towards a tradet View of Theory of Computing".
- The flynomistics for Computing Receipting awarded tim the principlaw Park population Reard is 2000 For the work on polyconial time reprint polyconstruct. For inter programmics.







Dr Narendra Karmarkar Dr Sharadchandra Shrikhande. Dr Jayant Narlikar.



Bapudev Sastri

Dattatreya Kaprekar 1905 - 1984

HARSHAD NUMBERS (Joyous Numbers) 12, 18, 20,

DEMLO NUMBERS (1, 121, 12321, 1234321 = Sq of 1, 11, 111, 1111 etc)

KAPREKAR NUMBERS (45X45, 55X55, 99X99); 703, 5292, 45X45 = 20 25 & 20+25 = 45 55X55 = 30 25 & 30+25 = 55 99X99 = 98 01 & 98 + 01 = 99; 703X703 = 494 209 & 494+209 = 703

DATTATREYA NUMBERS 7, 13, 35, 65 are Dattatreya Nos $13^2 = 13X13 = 169 = 16 * 9 = 4^2 * 3^2$ $7^2 = 7X7 = 49 (2^2, 3^2),$ $19^2 = 361 = 36 - 1 = 6^2 * 1^2$ $35^2 = 1,225 = 1 - 225 = 1^2 * 15^2$ $57^2 = 324 - 9 = 18^2 * 3^2,$ 16 $65^2 = 4,225 = 4 - 225 = 2^2 * 15^2,$



Dattatreya Kaprekar 1905 - 1984 Harshad Numbers Joyous Numbers

Numbers divisible by the sum of their digits

The first 50 Harshad numbers with more than one digit in base 10 are:

10, 12, 18, 20, 21, 24, 27, 30, 36, 40, 42, 45, 48, 50, 54, 60, 63, 70, 72, 80, 81, 84, 90, 100, 102, 108, 110, 111, 112, 114, 117, 120, 126, 132, 133, 135, 140, 144, 150, 152, 153, 156, 162, 171, 180, 190, 192, 195, 198, 200.

Dattatreya Kaprekar 1905 - 1984 Demlo Numbers Demlo is a Railway Station in India



numbers 1, 121, 12321, 1234321..., which are the squares of the repunits 1, 11, 111,



<u>Dattatreya Kaprekar 1905 - 1984</u> <u>Kaprekar Numbers</u>

a positive integer with the property that if it is squared, then its representation can be partitioned into two positive integer parts whose sum is equal to the original number

 $45 \times 45 = 20\ 25\ (20 + 25 = 45)$ $55\ X\ 55 = 30\ 25\ (30 + 25 = 55)$ $703^2 = 494\ 209\ (494 + 209 = 703)$ $2728^2\ =\ 744\ 1984\ (744\ +1984)$ $5292^2 = 28\ 005264\ (28 + 00\ 5264)$ $857\ 143^2\ =\ (734\ 694\ +\ 122\ 449)$

 $99^2 = 98\ 01\ (98 \div 01 = 99)$



Dattatreya Kaprekar 1905 - 1984 Devlali Numbers (Self Nos) Kaprekar lived in Devlali

Integers that cannot be generated by taking some other number and adding its own digits to it.

 20
 is
 a
 SELF
 No.

 21 is NOT a Self No. 21 = (15 + 1 and 5 ie: 15 + 1 + 5 = 21



<u>Dattatreya Kaprekar 1905 - 1984</u> <u>Dattatreya Numbers</u>

- Numbers of the Form D = Wn A + B
- Where D, A, B are Squares
- $13 \times 13 = 169 = (16 \& 9 ie 4^2 and 3^2)$
- $13^2 = 4^2 \& 3^2 = 10X 4^2 + 3^2$

D = Wn A + B D, A & B are Square Numbers

In Decimal System D = 10A + B(D, A, B are Squares) 49, 169, 361, 1-225, 324-9, 4-225,

Srinivas Ramanujam 1887 – 192



'in the same league as legendary mathematicians such as Gauss, Euler, Newton and Archimedes' Cauchy,

English mathematician G.H. Hardy



Died at the age of 32. Fellow of Royal Society, Fellow of Trinity College, Cambridge



Ramanujan Number = $10^3 + 9^3 = 12^3 + 1^3$ 1729 Mathematical analysis, Number Theory, **Infinite Series** and

Continued Fractions.

3900 results

(mostly identities and equations) independently compiled results - both original and highly unconventional Ramanujan prime and the Ramanujan theta function,

<u>Akshay Venkatesh 1981</u> <u>Perth, Western Australia</u>



International Physics Olympiad and International Mathematics Olympiad, at the age of 12 only Australian to win 2 Olympiads

Stanford University



Professor

counting, equi-distribution problems in auto-morphic forms and number theory, in particular representation theory, locally symmetric spaces and ergodic theory.

Ancient Books of Vedic Knowledge

4 Vedas	6 Vedangas	4 Upa Vedas	4 Upangas
• Rig	 Siksha (Phonetics) Vyakarana (Grammer) 	 Ayurveda (Charak Samhita) 	• Mimamsa (Jaimini)
• Yajur	• Chhandas (Metres)	• Dhanurveda (Vishwamitra)	 Nyaya (Rishi Gautam)
• Sama	 Niruktam (Etymology – origin of words) 	 Gandharva Veda (Bharat Muni) 	 Puranas (Ved Vyas)
• Atharva	 Jyotisham (Astronomy- Eye of Ved) Kalpam 	 Stapathya Veda & Artha Shastra (Bhrugu Ved Vyas) 	 Dharma Shastras (Manu, Parashar, Yajnavalkya etc)
	• Kalpam (ceremonies- limbs of Ved) Le	t Noble Thoughts come from all directions. Rig Veda	2



Jyotis-Sashtra Surya Bhagwan Taught Mayan Aryabhatta, Varahamihir, Bhaskaracharya

Sidhanta Skanda Vyakta Ganit Avyakta Ganit Sameekaran Hora Skanda Horoscope 12 Zodiac Signs Samhita Skanda Sagunas, Nimitta Scents

Vedic Physics					
Measurement of Time					
÷	Vedic Units of Time				
÷	(a) Smaller Units of	Time	3		
÷	TRUTI	= 33,	750th	fraction	of a
	second is the smallest	unit	of time	e	
÷	• 100 Truti •	= 1	Tatpar	a	
÷	45 Tatpara = 1	Nimes	sha		
÷	30 Nimesha =	= 1	Prana	=	4 secs
÷	\sim 3 Nimesh = 1 \land	Vipala	3	= 0.4 s	econds
÷	\sim 60 Vipalas = 1	Pala	= 24	seconds	5
÷	60 Palas = 1 (Ghatil	ka	= 24 M	inutes
÷	60 Ghatikas = 1	Divas		= 1 day	/ or 24
	Hours			•	

Vedic Physics Measurement of Time

\	Vedic Units of Tim	<u>)e</u>	
\	(a) Larger Units	of Time	
\	7 Divas	= 1 Saptah	= 1 week
\	15 Divas	= 1 Paksha	= 1 Fortnight
\	2 Paksha	= 1 Maas	= 1 Month
÷	2 Maas	= 1 Ritu	= 1 Season
÷	6 Maas	= 1 Ayana (Uttaraya	n & Dakshinayan)
\	6 Ritu = 2 Ay	anas = 12 Maas =	1 Varsha = 1 Year
	12 Years	= 1 Kumbha	
	60 Years	= Sashtiyapta	i Purti
÷	100 Years	= 1 Shatabda	
\	10 Shatabda	= 1 Sahasrabda	= 1 Millenium =
	1,000 years		

	Vedic	Physics		CARL SAGAN Cosmos -	
	Meası	irement	of Ti	Me TV Serial	20
* *	<u>Vedic Units</u> (b) Highe	<u>s of Time</u> r Units of Time			
	432 Sahasra 2 Yuq	bda = 1 Kali Yug o = 1 Dwapar Yug	rYug = =	432,000 years	
•	3 Yug	= 1 Treta Yug	=	1296,000 years	
	4 Yug 10 Yug	= 1 Satya Yug = 1 Maha Yug	=	4.32 Million Years	
* *	1000 Maha Y 2 Kalpa = 360 Days of	'ug = 1 Kalpa 1 Day of Brahma Brahma = 1 Ye	= 4.32 Billi = 2,000 Ma ear of Brahma	ion Years = Morning aha Yug = 8.64 Billior a = 3110.4 Billi	of Brahma Years on Years
1	<u>Maha Kalpa</u> o	r <u>Brahma Ayu</u> = 1 =	LOO Years of 311.04 Tril	= 3.1104 Trillio Brahma Ilion Years	on Years
*		=	3.1104 X 1 <u>311,040</u>	014 Solar Years ,000,000,000 sola	n r years .
	Thus the Vedic <u>TRUTI</u>	Seers had thought of , the smallest Unit of 1	the smallest a Time =	nd the largest units of tim <u>33,750th part of a S</u>	e namely, ' <u>econd</u>

- TRUTI, the smallest Unit of Time
- Maha Kalpa or Brahma Ayu, +

÷

= <u>311,040,000,000,000 solar years</u>, the largest Unit of Time

European Equivalents

Indian inventions

1. Bodhayan(BC 1700 / 800 BCE) Diagonal square theorem

Professor H. G. Rawlinson writes:

Foreigners` claims

Pythagoras theorem (BC 540)

It is more likely that Pythagoras was influenced by India than by Egypt. Almost all the theories, religions, philosophical and mathematical taught by the Pythagoreans, were known in India in the sixth century B.C., and the Pythagoreans, like the Jains and the Buddhists, refrained from the destruction of life and eating meat and regarded certain vegetables such as beans as taboo" "It seems that the so-called Pythagorean theorem of the quadrature of the hypotenuse was already known to the Indians in the older Vedic times, and thus before Pythagoras (ibid). (Legacy of India 1937, p. 5).

Indian inventions

2. Varahamihir (488-587AD) Tri-Lostaka European Equivalents

Foreigners` claims

B.Pascal (1623-1662 AD) Pascal triangle.

Chandas Shastra an Ancient Indian book on Sanskrit prosody written by Pingala between the 5th and 2nd century BCE.

While Pingala's work only survives in fragments, the commentator Halayudha, around 975, used the triangle to explain obscure references to *Meru-prastaara*, the "Staircase of Mount Meru".

Foreigners` claims

Indian inventions

3. Brahmagupta (628 AD) N x^{2} + 1 = y^{2}

Foreigners` claims

John Pell (1610-1685) Pell`s equation.

Pell's equations were studied as early as They were mainly interested in the equation 1000 BC in India.

 $X^2 - 2Y^2 = 1$

because of its connection to the square root of two. Indeed, if x and y are integers satisfying this equation, then x / y is an approximation of $\sqrt{2}$. For example, **Baudhayana** discovered that

x = 17, *y* = 12 & *x* = 577, *y* = 408

are two solutions to the Pell's equation, and give very close approximations to the square root of two.

Indian inventions

4.Virahank`s (600AD) series 0,1,1,2,3,5,8,13,21.....

European Equivalents

European Equivalents

Fibonacci series (1170-1250)

The Fibonacci sequence was well known in ancient India, where it was applied to the metrical sciences (prosody), long before it was known in Europe.

Developments have been attributed to <u>Vedic Scholar Pingala</u> (400 BC), <u>Virahanka</u> (6th century AD), <u>Gopāla</u> (c.1135 AD), and <u>Hemachandra</u> (c.1150 AD).

The motivation came from <u>Sanskrit prosody</u>, where long syllables have length 2 and short syllables have length 1. Any pattern of length n can be formed by adding a short syllable to a pattern of length n - 1, or a long syllable to a pattern of length n - 2; thus the prosodists showed that the number of patterns of length n is the sum of the two previous numbers in the sequence. <u>Donald Knuth</u> reviews this work in <u>The Art of Computer</u> <u>Programming</u>.

Foreigners` claims

5. Mahavira formula(850 AD) Herigone`s formula(1634 AD) for combinations n Cr = (n)! / (r!) (n-r)! (!stands for factorial)

6 Bhaskaracharya (1114-1193) Rolle`s theorem(1652-1719) Formula for relative difference (retrograde motion)

7. Madhav`s theorem (1340-1425) Gregory Series(1638-1675) x = tan x / 1 – tan 3 x / 3 + tan 5 x / 5 -

8. Madhav`s series **(1340-1425)** II (pie) = 1-1/3 + 1/5 - 1/7 +..... Leibnitz `s expansion (1646-1716)

9. Narayan Pandit (1356 AD) Fermat`s result (1601-65) factorization method for divisiors of a number

10. Bhaskaracharya (1114-1193) Euler's division algorithm method of finding greatest common divisor

11. Permeshwara`s (1360 AD)Huiler`s formula (1782AD)Formula for finding circum-radius of a cyclic quadrilateral

Foreigners` claims

12. Nilkanth Somyaji (1444-1545) Summations $\sum n$, $\sum n^2$ and $\sum n^3$

13 Nilkanth Somyaji (1444-1545) r sine rule a / sin A = b / sin B = c / sin C

14. Brahmagupta (628 AD volumes of frustum of cone and of pyramid

15 Jyeshtha Deo (1500 AD) formulae for sin(x+y) and cos(x+y) in the text `Yuktibhasha`

16 Jyeshtha Deo (1500 AD), Linear equations,

17 Jyeshtha Deo (1500 AD) volume and surface area of a sphere

18. Shankar Variar (1500-60) Values of II/4, II/16 in series

Euler`s results (1707-1783)

Euler's results

Kepler

Euler

Liebnitz (1646-1716)

Liebnitz, by method of integration

Gauss(1777-1855)

<u>MATHEMATICIAN TIME PERIOD</u>

- Baudhayana (1700 / 800 B.C.E. 1st to explain Pythagoras Theorem)
- Apastamba (1500 / 600 BCE)
 Katyayana (1100 / 200 BCE) Umaswati (150 B.C.E.)
- Aryabhata (476-c. 550 C.E.)
 Varahamihira (c. 505-c. 558)
 Brahmagupta (c. 598-c. 670)
 Govindaswami (c. 800-850)
 Mahavira (Mahaviracharya) (850)

MATHEMATICIAN TIME PERIOD

Pruthudakaswami (850) Sridhara (900) Manjula (930) Aryabhata II (950) Prashastidhara (958) Halayudha (975) Jayadeva (1000)
MATHEMATICIAN TIME PERIOD

- Sripathi (1039) Hemachandra Suri (b. 1089) Bhaskara (1114-c. 1185) Cangadeva (1205) Madhava of Sangamagramma (C. 1340 - 1425)Narayama Pandit (1350)Paramesvara (1360-1455)
- Nilakantha Somayaji (1455-1555)
 Let Noble Thoughts come from all directions. Rig Veda

<u>MATHEMATICIAN TIME PERIOD</u>

- Sankara Variar (c. 1500-1560)
 Narayana (c. 1500-1575)
- Jyesthadeva (550)
- Acyuta Pisarati (c. 1550-1621)
 Putumana Somayaji (c. 1660-1740) Jaganath Pandit (1700)
- Sankara Varman (1800)

Vedic Additions

- 300 + 40 + 5**39 30 + 9** 345 Ι 46 I 678 40 + 6 600 + 70 + 8Ι 70+15 = **85** I 10 23 900 + 110 + 1385
- I 900 + 120 + 3 I = 1023

346	300	+	40	+	6
987	900	+	80	+	7
123	100	+	20	+	3
805	800	+	00	+	5

22 61 2100 + 140 + 21

22 6 1

Vedic Additions

			Hundred s	Tens	Units
	0346		300	40	6
+	0987		900	80	7
+	0123		100	20	3
+	0805		800	00	5
TOTAL	<mark>22 6 1</mark>	Total	2100	140	21
		=	2100	160	1
			2200	60	1
TOTAL			<mark>22</mark>	<mark>6</mark>	1

Vedic Subtractions

 are * If any digit in the SECOI 1 and 9 FIRST LINE), then we find FIRST LINE 	nd its MITRA and add it to the digit in
 3 and 7 4 and 6 5 and 5 Add 1 to the left of the Add Green Numbers 	e Mitra number and <mark>Subtract PINK</mark> numbers

				24 from 53				
First Line	ľ,	5	3	4 (of 24) is bigger than 3 (of 53)	53		5	3
Second Line	-	2	4	MITRA of 4 is <mark>6</mark> 6 + 3 = 9	- <mark>A</mark> 6	-	<mark>3</mark>	+ <mark>6</mark>
				Add 1 to 2 (of 24) =3		=	2	9
				5 - 3 = 2				

Vedic Subtractions

MIT <u>RAS</u>
are
1 and 9
2 and 8
3 and 7
4 and 6
E and E

a 1 (1

Compare the digits in the First Line and Second Line. * If any digit in the SECOND LINE is bigger (than the digit in the FIRST LINE), then we find its MITRA and add it to the digit in FIRST LINE

- Add 1 to the left of the Mitra number
- Add Green Numbers and Subtract PINK numbers

		To Subtract 274 from 523		
First Line	523	4 (of 274) is bigger than 3 (of 573)	523	523 2.74
Second Line	-274	MITRA of 4 is 6 Add 1 to 7 = 8 Mitra of 8 = 2	-286	- <mark>3</mark> +2+6
Answer	249		Answer	<mark>=2 4 9</mark>
		Add 1 to 2 (of 274) =3		
		5 - 3 = 2		

Vedic Subtractions

		To Subtract 256 524 from 975 708
First Line	975708	Bigger Nos 6 and 2
		Mitras <mark>4</mark> and <mark>8</mark>
Cocord Line		Add 1 to Nos on Left
Second Line	- 256 524	Subtract Pink Nos
Redesigned 2 nd Line	975 708	
	256 524	
	2 <mark>6 4 6 8</mark> 4	
Answer	<mark>719 184</mark>	

Multiplying by 5

- Case 1: All Even Digits
- Case 2: Odd and Even Digits{last Digit is even}
- Case 3: Odd and Even Digits {last Digit is odd, including all odd digits}

<u>Multiplying by 5</u> <u>– All Even Digits</u>

- Step 1: Divide by 2
 Step 2: Add a Zero
- Example: 5 x 4
- Step 1: Divide 4 by 2 = 2
- Step 2: Add Zero = 20
- Example: $5 \times 12 = 6 / 0 = 60$

<u>Multiplying by 5 – All Even Digits</u>



- Example: 5 X 2 5 6
- Step 1 : Put a dot below all odd numbers
- Step 2 : Subtract one from all odd Digits to make them EVEN and write this Even Digit above the Odd Digit
- Step 3 : Carry Forward this one to the Digit on the Right of the Odd Digit
- Step 4 : Divide each Digit by 2 and Add Zero

Example: 5 X 2 3 6 9 4

Step 1 : Put a dot below all odd numbers

2 3.6 9.4

Step 2 : Subtract one from all odd Digits to make them EVEN and write this Even Digit above the Odd Digit

2²3.6⁸9.4

Let Noble Thoughts come from all directions. Rig Veda

→ 5 X 2 3 6 9 4

Step 3 : Carry Forward this one to the Digit on the Right of the Odd Digit

Step 4 : Divide each Digit by 2 and Add Zero

Answer

Solve

- $\Rightarrow 5 X 2 3 4 = 2-2-14 x5$ = 1170
- $\Rightarrow 5 X 2 0 3 0 4 = 2 0 2 10 4 \times 5 = 1 0 1, 5 2 0$
- → 5 X 2 0 0 3 0 0 4 = 2-0-0-2-10-0-4 = 10,015,020
- → 5 X 4 ,3 5 6 ,7 7 8
 - = 4-2-14-16-6-16-18x5
 - = 21, 783, 890

 \Rightarrow 5 X 1 2 ,3 4 5 ,6 7 8 = 61,728,390

<u>Multiplying by 5 – All Odd Digits</u>

- 357 Example :
- → Step 1 :
- Subtract one from all Odd Digits and make them Even
- \rightarrow Step 2 : Carry forward this one to the Digit on Right side
- Divide by 2 and add <u>~~</u> → Step 3 :

Multiplying by 5 – All Odd Digits

→ Example : 3 5 7 x5

 Step 1 : Subtract one from all Odd Digits and make them Even
 2 4 6 *

→ Step 2 :

→ Step 3 :

Carry forward this one to the Digit on Right side $2_{1}4_{1}6$ * Divide by 2 and add 5'' 1785

Multiplying by 5 – All Odd Digits

Solve → 5 X 3 5 7 9 = 2-14-16-18-* = 17,895 → 5 X 9 7 5 3 = 8-16-14-12-* = 4 8, 7 6 5 \Rightarrow 5 X 1 3 0 7 9 = 12-10-6-18-*= 6 5, 3 9 5 → 5 X 3 0 5 5 7 7 = 2-10-4-14-16-16-* = 1 5 2 7 8 8 5 = 1,527,885→ 5 X 999 777 555 = 8-18-18 - 16-16-16 - 14-14-14-* = 499 888. 777 5 5 X 303 507 7009

<u>Multiplying by 5 – Any Number</u>

◆Solve
◆5 X 2 3 5 8
◆5 X 1 2 3 0 5 6
◆5 X 2 3 4 5 6 7 8 9
◆5 X 1 2 3 4 5 6 7 8 9
◆5 X 9 8 7 6 5 4 3 2 1

To Multiply by 11

Clue: Add adjacent numbers

→ Step 2:

Step 3:

- Step 1: write the the first and last digit as they are
 - Add two adjacent digits from the right and fill the gaps
 - Carry forward 1 if need be to the left

To Multiply by 11 – No Carry Forward

→ Example: 11 X 24

Step 1: write the the first and last digits as they are

→ 2 <u>N</u> 4

Step 2: Add two adjacent
 digits from the right
 and fill the gaps
 2 6 4 (2 + 4 = 6)

To Multiply by 11

→ Example: 11 X 17

- Step 1: write the the first and last digits as they are
 1 N 7
- Step 2: Add two adjacent
 digits from the right
 and fill the gaps
 1 8 7 (1 + 7 = 8)

To Multiply by 11

Solve: (answers are in BLUE) $\rightarrow 11 \times 22 = 242$ $11 \times 33 = 363$ $\rightarrow 11 \times 27 = 297$ $11 \times 36 = 396$ $\rightarrow 11 \times 44 = 484$ $11 \times 54 = 594$ $11 \times 72 = 792$ **→11 X 62 =<mark>682</mark> →11 X 81 =891** $11 \times 71 = 781$

To Multiply by 11 – Carry Forward

- Example:11 X 38
- \rightarrow Here 3 + 8 = 11. Hence Carry forward
- Step 1: write the the first and last digits as they are
- → 3 <u>N</u> 8
- Step 2: Add two adjacent digits from the right and fill the gaps
 - 4 1 8 (3 + 8 = 11)

<u> To Multiply by 11 – Carry Forward</u>								
<pre>Solve: Answers are in BLUE</pre>								
→ 11	X	29	= <mark>319</mark>	11	X	39	=	<mark>439</mark>
→11	X	48	= 528	11	X	68	=	748
→11	X	99	=108	9 11	X	88	=	968
→11	X	76	<mark>=836</mark>	11	X	67	=	737
→11	X	85	= <mark>935</mark>	11	X	58	=	638

<u>To Multiply by 11 – 3 or more Digits</u>

→ Example: 11 X 2 3 4

- Step 1: write the the first and last digits as they are
- → 2<u>NM</u>4
- Step 2: Add two adjacent digits from the right and fill the gaps
- $\begin{array}{rcl} \bullet & 2/(2+3)/(3+4)/4 \\ &= 2 5 7 4 \end{array}$

<u>To Multiply by 11 – 3 or more Digits</u>

→ Example: 11 X 2 6 1 3 4

Step 1: write the the first and last digits as they are

→ 2 <u>N M P Q 4</u>

Step 2: Add two adjacent digits from the right and fill the gaps

→ 2/(2+6)/ (6+1)/ (1+3)/ (3+4)/ 4

2 <u>8 7 4 7</u> 4

<u>To Multiply by 11 – 3 or more Digits</u> with Carry Forward

→ Example: 11 X 2 8 1 9 4

- Step 1: write the the first and last digits as they are
- → 2 <u>N M P Q 4</u>
- Step 2: Add two adjacent digits from the right and fill the gaps
 - 2/ (2+8)/ (8+1)/ (1+9)/ (9+4)/ 4 2 / 10/ 9 / 10/ 13/ 4

3 <u>1 0 1</u> <u>3</u> 4

To Multiply by 11 – Carry Forward

- Solve: Answers are in BLUE
- \Rightarrow 11 X 2709 = 29,799
- $11 X 3509 = \frac{38,599}{38}$
- →11 X 45318
 11 X 62815
- ↓11 X 8272 = 8/10/992 = 90,992
- ♦11 X 72635
 11 X 1234567
- →11 X 987654 11 X 9080706

To Divide 1 by 19, 29, 39, 49, ...99 Sutra is EKADHIKENA (One More) $1 \div 19 = 0.05263 1578 94736 8421$ $1 \div 29 =$ 0.0344 8275 862 068 9655 1724 137 931 Ekadhik or One More or Add One For dividing by **19** the multiplier is 2 3 For dividing by 29 the multiplier is For dividing by 59 the multiplier is 6 For dividing by 99 the multiplier is * When dividing by 19, the **BIGGEST REMINDER** is **18** (19 or 20 cannot be the reminders)

To Divide 1 by 19, 29, 39, 49, ...99 **COMPLIMENTS of 9:** 0&9, 1&8, 2&7, 3&6, 4&5 $1 \div 19 = 0.05263 1578 94736 8421$ $1 \div 19 = 0.052 631 578$ (There is a pattern) 947 368 421 (Complement of 9) $1 \div 19 = 0.052$ 631 **578** (PI Remember this) **947** 368 421 $1 \div 29 = 0.0344 8275 862 068$ 9655 1724 137 931 $1 \div 29 = 0.0344$ 8275 862 068 **55** 1724 **137** 931

Vedic Division: Divide 1 by 19, 1 Divided by 19, (VM says Multiply by 2)

Vedic Multiplication VM of 1 or 2 digits by 2:

VM of	16	is	6x2 +1	=	13
VM of	13	is	3x2 +1	=	7
VM of	7	is	7x2+0	=	14
VM of	14	is	4x2 +1	=	9
VM of	9	is	9x2	=	18
VM of	18	is	8x2 +1	=	17
VM of	17	is	7x2 +1	=	15
VM of	15	is	5X2 +1	=	11
VM of	11	is	1x2 +1	=	3
VM of	3	is	3x2	=	6
VM of	6	is	6x2	=	12

A. 1 Divided by 19, (VM says Multiply by 2) B. 1 ÷ 20 = 0.05 Hence 1 ÷ 19 should be close to 0.05 (& slightly bigger)

C. Write the answer from Right to Left by continuously multiplying by 2 starting with 1.

D. Vedic Multiplication of 1 or 2 digits by 2

E. $1 \div 19 =$

 $0.05_{1}2 \ 6 \ 3_{1}1_{1}5_{1}7_{1}8 \ 9_{1}4 \ 7_{1}3_{1}6 \ 8-4-2-1$

Multiply by 2 1 1X2 = 2 2X2 = 4 4X2 = 8 8X2 = 16 = 16

Vedic Multiplication by 2 $16X2 = {}_{1}6X2 = 12+1 = 13 = {}_{1}3$ ${}_{1}3x2 = 3X2 + 1 = 7$ $7X2 = 14 = {}_{1}4$ ${}_{1}4X2 = 4x2 + 1 = 9$ Vedic Multiplication by 2 $9X2 = 18 = {}_{1}8$ ${}_{1}8x2 = 8x2 + 1 = 17 = {}_{1}7$ ${}_{1}7x2 = 7x2 + 1 = 15 = {}_{1}5$ ${}_{1}5x2 = 5x2 + 1 = 11 = {}_{1}1$ ${}_{1}1x2 = 1x2 + 1 = 3$ A. 1 Divided by 19, (VM says Multiply by 2)

E. $1 \div 19 =$

 $0.05_{1}2 \ 6 \ 3_{1}1_{1}5_{1}7_{1}8 \ 9_{1}4 \ 7_{1}3_{1}6 \ 8-4-2-1$

F. 0. 0 5 2 6 3 1 5 7 8 9 1 4 7 1 3 6 8 4 2 1

G. 1 ÷ 19 = 0.052 631 578 947 368 421

Multiply by 2Vedia1Vedia1X2 = 216X22X2 = 413x24X2 = 87X2 =8X2 = 16 = 1614X2

Vedic Multiplication by 2 $16X2 = {}_{1}6X2 = 12+1 = 13 = {}_{1}3$ ${}_{1}3x2 = 3X2 + 1 = 7$ $7X2 = 14 = {}_{1}4$ ${}_{1}4X2 = 4x2 + 1 = 9$ Vedic Multiplication by 2 $9X2 = 18 = {}_{1}8$ ${}_{1}8x2 = 8x2 + 1 = 17 = {}_{1}7$ ${}_{1}7x2 = 7x2 + 1 = 15 = {}_{1}5$ ${}_{1}5x2 = 5x2 + 1 = 11 = {}_{1}1$ ${}_{1}1x2 = 1x2 + 1 = 3$

Square of Numbers ending in 5 Ekadikena Purvena (One More than Previous)

To Find (15)², (25)², (35)², ... (95)², (105)², (195)², (995)²,

EKADHI	KENA or One M	lore or A	dd 1
In case of	25 Add 1 gives	2 x 3	= 6
In case of	35 Add 1 gives	3 x 4	= 12
In case of	45 Add 1 gives	4 x 5	= 20
In case of	75 Add 1 gives	7 x 8	= 56
In case of	95 Add 1 gives	9 x 10	= 90
In case of	105 Add 1 gives	10 x 11	=110
In case of	195 Add 1 gives	19 x 20	= 380
In case of	995 Add 1 gives	99 x 100	= 9900

Square of Numbers ending in 5 Ekadikena Purvena (One More than Previous)

To Find Squares of 15, 25, 35, ... 95, 105, 195, 995,

 $(25)^2 = 6\ 25 \ (2x3 = 6) \ (5\ x\ 5 = 25)$

 $(105)^2$

 $(195)^2$

 $(35)^2 = 1225$ (3x4 = 12 & 5x5 = 25)

 $(85)^2 = 7225$ (8x9 = 72)

= 110 25 (10x11=110)

= 380 25 (19x20 = 380)

 $(995)^2 = 9900 25 (99x100 = 9900)$

Special Multiplications Ekadikena Purvena (One More than Previous) **SPECIAL CASES 2 conditions** (a) Units add to 10 & (b) Tens are same $23 \times 27 = 621 (2\times 3; 3\times 7) (3+7=10)$ $192 \times 198 = 380 16$ (19x20; 2x8) (19 is common & 2+8 = 10)**23 x 26 is not possible because units** 3+6=9 23 x 37 is not possible because TENS are 2 and 3 Find: 44x46=? (2024) 91x99 = (90 09) how !!

993x997 =? (<mark>9900 21</mark>) 84x86= ? (<mark>72 24</mark>)
Multiple Digits entirely of 9 Eka Nyunena Purvena (One Less than Previous) Step 1: Minus 1 Step 2: Complement from 9 **COMPLIMENTS of 9:** <mark>0&9, 1&8</mark>, 2&7, <mark>3&6,</mark> 4&5 Find $49 \times 99 =$ Step 1: Subtract 1 from 49 = 48Take complement of 4 & 8 = 51Step 2: 49 X 99 = 48 51 Hence 76x99 = 75 24; 123x999 = 122 877

Multiple Digits entirely of 9 Eka Nyunena Purvena (One Less than Previous) 49 X 99 = 48 51 777 x 999 = 776 223 $120\ 357\ x\ 999\ 999 =$ 120 356 - 879 643 879-643 $77 \times 999 = 077 \times 999 = 078 - 921$ $777 \times 99 = (776 \ 99 - 7 \ 76)$ = 76 9 23 $1234 \times 9 = (1233 \ 9 - 123 \ 3)$ = 11106 $1234 \times 99 = (1233 \cdot 99 - 1233) = 122,166$ $1234 \times 999 = (1233 \ 999 - 1233) = 1232,766$ (Subtract 1; adjust 99s on Rt side; subtract) General Multiplication Urdhva Tiryak (Vertical & Cross-wise)

 $12 \times 13 = 1 \times 1 / 1 \times 2 + 1 \times 3 / 2 \times 3$ = 1 / 2 + 3 / 6 = 156

37 x 42 = 12 / 28 + 6 / 14 = 12 / 34 /14 = 15 5 4

1021 x 2103 = 2/ 1/ 4/ 7/ 1/ 6/3 = 2147163

Tatitreeya Samhita 7-2-20-1 in 100 BCE

- 1 Ekam
- 10 Dasham
- 100 Shatam
- 10³ Sahasram
- 10⁵ Lakshaha
- 10⁷ Kotihi
- 10⁹ Ayutam
- → 10¹¹ Niyutam
- → 10¹³ Kankaram
- → 10¹⁵ Vivaram

 → 10¹⁷
 → 10¹⁹
 → 10²¹
 → 10²³
 → 10²⁵
 → 10²⁷
 → 10²⁹

 10^{31}

1033

Parardhaha Nivaahaha Utsangaha Bahulam Naagbaalaha Titilambham Vyavasthaana Pragnaptihi Hetuheelam Karahuhu

Tatitreeva Samhita 7-2-20-1 in 100 BCE

- → 10³⁵
- Hetvindreeyam
- → 10³⁷
 Samaapta lambhaha
- → 10³⁹ Gananaagatihi
- → 10⁴¹ Niravadyam → 10⁴³
 - Mudraabaalam
- → 10⁴⁵ Sarvabaalam
- → 10⁴⁷ Vishamagnagatihi → 10⁴⁹
 - Sarvagnaha
- → 10⁵¹ Vibhtangamaa
- → 10⁵³ Tallaakshanam

- In Anuyogdwaar Sutra
- → 100 BCE one
 numeral is raised as high as 10^{140}
- The highest prefix used for raising 10 to a power in <u>Today's Maths</u> is D for **10³⁰**

- Vedic Maths and Short Cuts as applied to Accountancy
- https://www.youtube.com/watch?v=m9pgirOIXdE
- •
- Accountancy applies a lot of mathematics. When we apply Vedic Mathematics to accountancy, calculations become simple and time saving. Thus
- Accountancy + Vedic Mathematics

= **MATHEMAGICS** of Accountancy.

- Technique 1: Dealing with Fractions and Percentages
- Case 1: Solutions of Problems dealing with Fractions
- Ans = <u>Fraction in Question</u> X Value Given
 Fraction Known

Let Noble Thoughts come from all directions. Rig Veda

- Case 1: Solutions of Problems dealing with Fractions
- Ans = <u>Fraction in Question</u> X Value Given
 Fraction Known
- Example 1:

If $\frac{1}{2}$ of my pocket money is Rs 500/- what is $\frac{3}{4}$ of my pocket money.

- Here Fraction in Question is $\frac{3}{4}$; Fraction Known is $\frac{1}{2}$
- Value Given for the known Fraction is Rs 500/-
- Hence Ans = $\{\frac{3}{4} / \frac{1}{2}\} \times 500$

=

=

- = (3x2)/(4x1) X 500
 - (3/2) X 500 = 3X250

<mark>Rs 750/-</mark>

% Known

Case 2: Solutions of Problems dealing with Percentage
 Ans = <u>% to Know</u> X Value Given

- Example 2: If 50% of my pocket money is Rs 500/- what is 75% of my pocket money.
- Here % to KNOW is 75% % Known is 50%
- Value Given for the known % is Rs 500/-

Hence, Ans = $(75/50) \times 500$ = Rs 750/-

- Example 3: I sold goods for Rs 50,000 at 25% profit on cost. What is the profit?
- Let 100x be the cost price. The Profit will be 25x and sale price will be 125x.
- Here value to KNOW is Profit which is 25%
- % Known is Sale Price = 125%. Sale Price value is Rs 50,000/-

•	Ans	=	<u>% to Kr</u> % Kno	<u>now</u> X wn	Value Given			
•	Ans = Profit	=	25%	X 50 000	= Rs 10 000/-			
•			<u>125%</u>	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,				
•	Ans:	=	<mark>Rs 10,0</mark>	00/-				
	Let Noble Thoughts come from all							

directions. Rig Veda

- Example 4: What is cost in the above example?
- Here we want to find the cost price which is 100%

•	Ans =	<u>% to Know</u> X Value Given
•		% Known
•	Ans = Cost Price =	<u>100%</u> X 50,000 = <mark>Rs 40,000/-</mark>
•		125%
•	Ans =	Rs 40,000/-

• Example 5: My father saves Rs 50,000 per month.

•	He spends	20 %	on	Rent
•		25 %	on	Household
•		20 %	on	Education
•		10 %	on	Sundries

- What is his total expense, What is his total income what is his expense on Rent, Household, Education and Sundries.
- Solution:

•

- To find his Total Expense
- His total expenses = 20% + 2
- Hence his Savings =
- Ans = His total Expense

20% + 25% + 20% + 10% = 75%

- 100 75 = 25% = Rs 50,000/-
- = <u>75%</u> x 50,000 = Rs 150,000/-25%

- Solution:
- His total Income = <u>100%</u> X 50,000 = Rs 200,000/-
- 25%
 His Expense on Rent = <u>20%</u> X 50,000 = Rs 40,000/-25%
- His expense on House Hold = 25% = Rs 50,000/-
- His expenses on Education = 20% = Rs 40,000/-
- His expenses on Sundries = 10% = Rs 20,000/-

Solution: ٠

•

- To find his Total Expense •
- His total expenses • =
- = Rs 50,000/-Hence his Savings 100 - 75 = 25%• =
- Ans = His total Expense <u>75%</u> x 50,000 = Rs 150,000/-• 25% •

20% + 25% + 20% + 10% = 75%

- His total Income = 100% X 50,000 Rs 200,000/-=
- 25% X 50,000 = His Expense on Rent 20% • = Rs 40,000/-
- 25% •
- His expense on House Hold =25% Rs = 50,000/-
- His expenses on Education = 20% Rs • = 40,000/-Let Noble Thoughts come from all
- directions. Rig1/09 His expenses on Sundries • _

Rs

- SHORT CUT TECHNIQUES
- Technique 2: To find Profit when CP or SP is given
- The Factors are Nr / (Dr+Nr) when Sale Price is Known
 - Nr / (Dr-Nr) when cost price is Known
 - Nr = Numerator Dr = Denominator
- Example 6: Sale of Goods is Rs 400/- at a Profit of 25% on Cost. What is the Profit.
- Answer: Profit is $25\% = \frac{1}{4}$ (Here Nr = 1 & Dr = 4)
- Hence the factor is Nr / (Dr+Nr) = 1/(1+4) = 1/5
- Multiply Sale by Factor = $400 \times 1/5$ = Rs 80/- is Profit.

- Example 7: Cost Price is Rs 30,000/- Profit is 40% on Sale
 What is the Profit
- Here the factor is Nr / (Dr-Nr) = 4/(10-4) = 4/6 = 2/3
- Hence Profit is cost X Factor = 30,000 X 2/3 = Rs 20,000/-
- Cross Check: CP + Profit = 30,000 + 20,000 = 50,000/-
- 40% on Sale is 50,000 X <u>4</u> = 20,000 correct Ans

- Technique 3:
- Example 8: I have Rs 4,000/- to invest in 2 Banks.
- SBI is paying 5% interest and BoB is paying 3% interest pa.
- Altogether I get Rs 288/- interest for 2 years.
- How much money to be invested in each bank?
- Solution:
- 1% on 4,000 = 40; Hence 5% // 3% will be 200 // 120
- The interest for 2 years is 288. Hence interest for 1 year is 144.
- If entire Rs 4,000 is invested in SBI // BoB, the interest for 1 year will be 200 // 120.
- But the interest was 144. The difference is 56 // 24
- Reverse is 24 // 56 Diving by 8 the Ratio is 3 // 7
- Hence the investment should be in the ratio of SBI // BoB :: 3 // 7 which is 400 X 3 // 400 X 7 = Rs 1200 // 2800
- Hence the investment should be Rs 1200 in SBI and Rs 2800 in BoB.

CROSS CHECK

•

- Interest by SBI at 5% on Rs 1200 for 1 year = 60
 - For 2 years = 120
- Interest by BoB at 3% on Rs 2800 = 84
- For 2 years = 168
- Hence total Interest for 2 years is 120 + 168 = Rs 288 Verified

• a

Let Noble Thoughts come from all directions. Rig Veda

Quote by SisterNivedita





Are the countrymen of Bhaskara & Sankaracharya inferior to those of Newton and Darwin? Sister Nivedita